

the cell is primitive, and there are no obvious systematic absences in  $hk0$  or  $0kl$  terms. There is only one  $h0l$  term (in which  $k+l=2n$ ), making no conclusion possible from these; in the cases where  $0k0$  and  $00l$  terms have  $k$  and  $l$  odd, acceptable duplicate indices are available, again making conclusions impossible.

Data for  $\beta$ -(NH<sub>4</sub>)<sub>2</sub>HPO<sub>4</sub> were given by Smith, Lehr & Brown (1957):  $a=8.03$ ,  $b=6.68$ ,  $c=11.02$  Å;  $\beta=113^\circ 38'$ ; 4 molecules per unit-cell, calculated density 1.61 g.cm<sup>-3</sup>. It is to be noted that  $c \sin \beta = 10.09$  Å, which compares with 10.78 Å for the  $a$  axis of the  $\alpha$  form, suggesting that this direction may remain common to both forms, merely expanding slightly. If the  $\alpha$  form had 8 molecules per unit cell, the calculated density would be 1.25 g.cm<sup>-3</sup>. The ratio of low-temperature-form density to high temperature-

form density is then 1.29, which compares with ratios of 1.24 and 1.20 for NH<sub>4</sub>Br and NH<sub>4</sub>Cl respectively.

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**Effect of wavelength on the sign of the photo-elastic constant ( $P_{11}-P_{12}$ ) of crystals of sodium-chloride structure.** By K. G. BANSIGIR, *Department of Physics, Osmania University, Hyderabad-7, India*

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A new method is presented for calculating the reversal wavelength at which the strain optical constant ( $P_{11}-P_{12}$ ) for alkali halides of sodium-chloride structure changes sign. Calculated absolute strain optical constants, their ratios and the strain polarizability constants of rubidium halides are given.

Bansigir & Iyengar (1961*a*) developed a theory of piezo-optic birefringence in cubic crystals of sodium chloride structure. The expressions obtained were:

$$(n^3/2)(P_{11}-P_{12})=3M-(1+\sigma)A \quad (1)$$

$$(n^3/2)(P_{11}+2P_{12})=(3L-A)(1-2\sigma) \quad (2)$$

and

$$(n^3/6)(P_{11}+2P_{12})=L(1-\lambda_0) \quad (3)$$

where

$$\lambda_0 = 2\sigma + A(1-2\sigma)/3L$$

$$M = (n^2-1)^2(n^2+5)/45n,$$

$$L = (n^2-1)(n^2+2)/6n$$

and

$$A = \frac{(n^2+2)^2(n^2+5)}{54n} \left[ 1.458 + 2.9005 \beta \left( \frac{1}{f_1} + \frac{1}{f_2} \right) \right] \times \theta^2 \\ - \frac{(n^2-1)(n^2+2)(n^2+5)}{18n} \left[ 2.916 + 4.2083 \frac{\beta}{f_1} \right. \\ \left. + 7.5927 \frac{\beta}{f_2} \theta \right] + \frac{(n^2-1)^2(n^2+5)}{3n} \left[ 0.2711 + 1.6922 \frac{\beta}{f_2} \right].$$

$P_{11}$  and  $P_{12}$  are the strain-optical constants,  $n$  the refractive index,  $\sigma$  Poisson's ratio,  $\beta$  the number of valence electrons,  $f_1, f_2$  the oscillator strengths,  $\theta = \alpha_j/r^3$  ( $\alpha_j$  is the polarizability of the  $j$ th ion and  $r$  is the interionic distance) and  $\lambda_0$  is the strain polarizability constant.

Using these expressions, Bansigir & Iyengar (1961*b*) calculated the wavelengths at which the photo-elastic constant ( $P_{11}-P_{12}$ ) changes sign for KCl, KBr and KI crystals. The method adopted is based on an empirical relation that  $\alpha_j/\alpha$  varies linearly with  $1/\lambda^2$  in the visible region ( $\alpha$  is the sum of the polarizabilities of the two types of ion and  $\lambda$  is the wavelength of light). If this empirical relation is used, one has to evaluate  $\alpha_j/\alpha$  for a large number of wavelengths from the observed photo-elastic constants ( $P_{11}-P_{12}$ ).

In this note a new method is given by which one can calculate the reversal wavelength at which ( $P_{11}-P_{12}$ ) changes sign, *i.e.* from a positive value to a negative value. In order to calculate the wavelength at which ( $P_{11}-P_{12}$ ) is equal to zero, equations (1) and (2) can be expressed in the following form:

$$x^3 + ax^2 + bx + c = 0 \quad (3)$$

$$\text{where } a = \frac{45}{2} \left( \frac{1+\sigma}{1-2\sigma} \right) P_{12} - \frac{15}{2} (1+\sigma) + 3$$

$$b = - \frac{15}{2} (1+\sigma) + 9$$

$$c = 15 (1+\sigma) + 5$$

and  $x = n^2$  (where  $n$  is the refractive index of the crystalline medium for which ( $P_{11}-P_{12}$ ) is equal to zero).

Therefore  $x$  or  $n$  can be evaluated if we know the Poisson's ratio and the photo-elastic constant  $P_{12}$  for the wavelength at which ( $P_{11}-P_{12}$ ) is equal to zero. For KCl, KBr and KI these wavelengths lie in the ultraviolet region (Srinivasan, 1959).

It is observed (Rahman & Iyengar 1966; Bansigir & Iyengar, 1961*b*) that the variation of the photo-elastic constant  $P_{12}$  is less than 5% for the entire wavelength range (from ultraviolet to the visible region). In view of this observation, one can evaluate the value of  $P_{12}$  approximately in the ultraviolet region from the observed value of  $P_{12}$  in the visible region.  $P_{12}$  of KCl, KBr, KI, RbCl, RbBr, and RbI in the ultraviolet region have been calculated by reducing the observed value at 5890 Å by 5%. Using these reduced values of  $P_{12}$ , refractive indices at the reversal wavelengths have been calculated and given in Table 1. Since dispersion data for KCl, KBr, KI and RbCl (Gyulai, 1927), RbBr and RbI (Kublitzky, 1932) are

available, the reversal wavelengths for these alkali halides have been calculated from the known refractive indices and given in Table 1, along with the observed ones (Srinivasan, 1959). It is found that the agreement is satisfactory.

Table 1. *Refractive indices and reversal wavelengths at which  $(P_{11} - P_{12}) = 0$ .*

Crystal	Refractive index, $n$	Reversal wavelength, $\lambda$	
		Calculated	Observed
KCl	1.584	2548 Å	2550 Å
KBr	1.690	2712	2760
KI	1.768	3370	3380
RbCl	1.693	2092	—
RbBr	1.681	2690	—
RbI	1.824	2938	—

Absolute strain optical constants  $P_{11}$  and  $P_{12}$ , their ratios and strain polarizability constants of rubidium halides have been calculated from the experimental data (Narasimha Murthy, 1960) and expressions 1, 2 and 3. Values thus obtained are given in Table 2.

Table 2.  $P_{11}$ ,  $P_{12}$ ,  $P_{12}/P_{11}$  and  $\lambda_0$ .

Crystals	$P_{11}$	$P_{12}$	$P_{12}/P_{11}$	$\lambda_0$
RbCl	0.288	0.172	0.597	0.3946
RbBr	0.293	0.185	0.631	0.4089
RbI	0.262	0.167	0.637	0.4412

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**The crystal and molecular structure of phosphorus tricyanide. Erratum.** By K. EMERSON *California Institute of Technology, Pasadena, California, U.S.A.*, and D. BRITTON, *University of Minnesota, Minneapolis 14, Minnesota, U.S.A.*

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Corrections to *Acta Cryst.* **17**, 1134 (1964).

It has been brought to our attention by Dr Tor Bjorvatten that there is an error in the text of our article on the structure of  $P(CN)_3$  (Emerson & Britton, 1964). On p. 1138 at the top of column 1, sentence 2 reads: 'The C-N-P angles for these atoms are  $116^\circ$ ,  $122^\circ$  and  $116^\circ$ , ...'. The cited angles should read  $155^\circ$ ,  $148^\circ$  and  $154^\circ$ . The significance of these angles lay in their departure from  $180^\circ$ ,

and our conclusions about the structure are still valid. We wish to thank Dr Bjorvatten for bringing this error to our attention.

#### Reference

- EMERSON, K. & BRITTON, D. (1964). *Acta Cryst.* **17**, 1134.